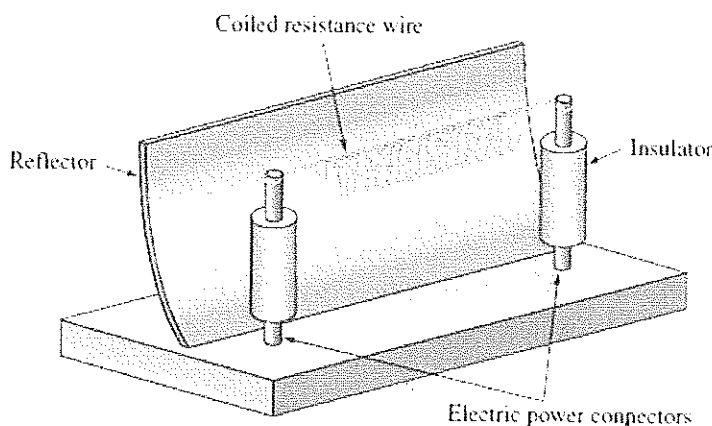


CANKAYA UNIVERSITY
 FACULTY OF ENGINEERING
 MECHANICAL ENGINEERING DEPARTMENT
 ME 313 HEAT TRANSFER

Fall 2016

HW 9

- 1) An electrical room heater consists of a horizontal coil of electrical resistance wire, as shown in figure given below. Such a coil is to be tested at a low power that will result in a wire temperature of 350°C . Calculate the rate of convection heat loss per unit length from the wire, which is 1 mm in diameter. For the purposes of this calculation, the wire can be approximated as being straight and horizontal. Room air is at 27°C . Repeat the calculation for a test performed in a carbon dioxide atmosphere, also at 27°C .



$$T_f = 27^\circ\text{C}$$

$$Ra_D = \frac{g\beta\Delta T D^3}{\nu^2} Pr = \frac{(9.81)(350)(100)(0.001)^3}{(2.12 \times 10^{-5})^2} (0.7)$$

$$= 4.43$$

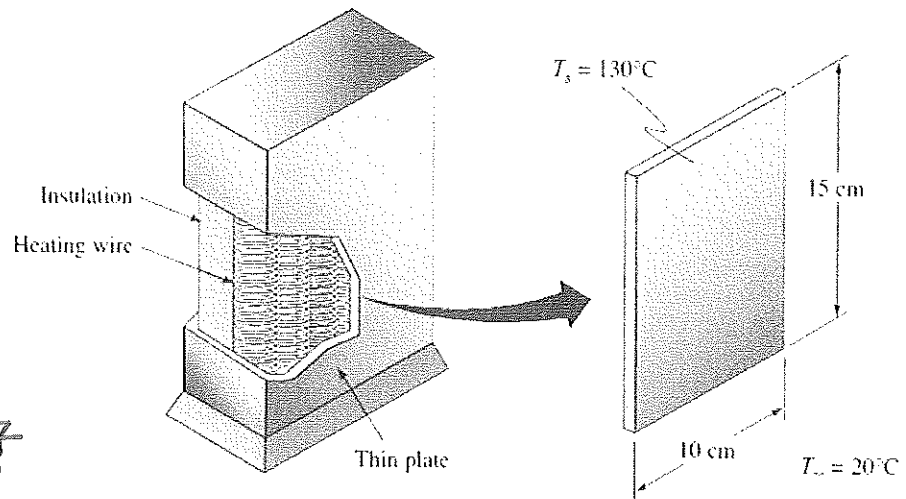
$$Nu_D = C Ra_D^n = 1.02 (4.43)^{0.148} = 1.27$$

$$\bar{h} = \frac{k}{D} Nu_D = \left(\frac{0.0291}{0.001}\right) (1.27) = 37 \text{ W/m}^2\text{K}$$

$$q = \bar{h} \pi D L (T_w - T_\infty)$$

$$q/L = \bar{h} \pi D (T_w - T_\infty) = (37)(\pi)(0.001)(100) = 11.61 \text{ W/m}$$

- 2) The rating for the small vertical-plate resistance heater shown in Figure given below is to be determined. Estimate the electrical power required to maintain the vertical heater surface at 130°C in ambient air at 20°C . The plate is 15 cm high and 10 cm wide. Compare with results for a plate 450 cm high. The heat transfer coefficient for radiation is $8.5 \text{ W/m}^2 \text{ K}$ for the specified surface temperature.



$$T_f = 75^\circ\text{C}$$

$$Gr_L \approx 2.41 \times 10^7$$

$Pr = 0.71$ for air

$$Gr_L Pr \approx 1.17 \times 10^7$$

$$Nu_L = C Ra_L^n$$

$$C = 0.59$$

$$n = 1/3$$

$$\bar{Nu}_L = 0.59 (1.17 \times 10^7)^{1/3} \approx 58$$

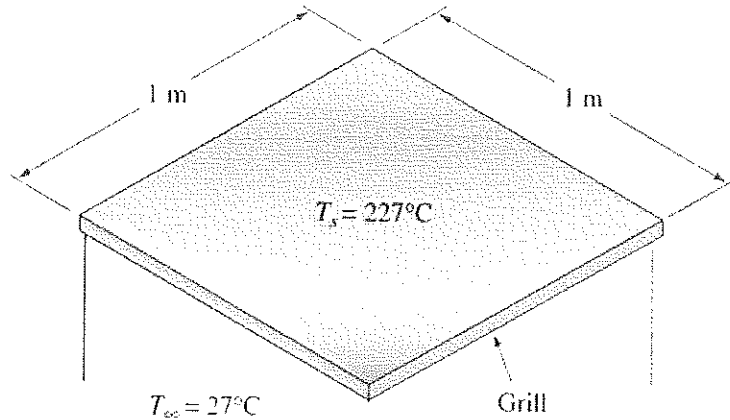
$$\bar{h} = \bar{Nu}_L \frac{k}{L} = (58) \left(\frac{0.029}{0.15} \right) = 11.3 \text{ W/m}^2 \text{ K}$$

$$q = A (\bar{h}_c + \bar{h}_r) (T_w - T_\infty)$$

$$= (2)(45)(0.1)(11.3 + 8.5)(110) = 1960 \text{ W}$$

3)

Calculate the rate of convection heat loss from the top and bottom of a flat, 1-m square, horizontal restaurant grill heated to 227 °C in ambient air at (see Figure)



$$L = \frac{A}{P} = \frac{L^2}{4L} = L/4 = 0.25 \text{ m}$$

use air properties
at T_f

$$Ra_L = \frac{(9.8)(200)(0.25)^3(0.71)}{(396)(2.7 \times 10^{-5})} = 7.55 \times 10^7$$

$$\overline{Nu}_L = 0.27(7.55 \times 10^7)^{0.25} = 23.2 \text{ for heat transfer from bottom of plate}$$

$$\overline{Nu}_L = 0.15(7.55 \times 10^7)^{0.33} = 63.4 \text{ from top surface.}$$

$$\overline{h} = 3.23 \text{ W/m}^2\text{K}$$

$$\overline{h} = 8.11 \text{ W/m}^2\text{K}$$

$$q = (1)(3.23 + 8.11)(200) = 2268 \text{ W}$$