

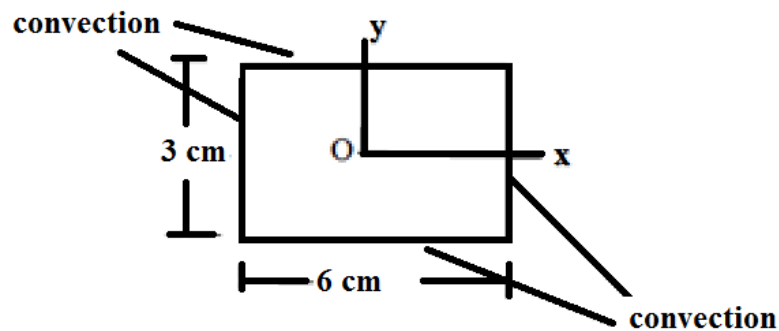
Cankaya University
Faculty of Engineering
Mechanical Engineering Department
ME 313 Heat Transfer

Chapter-5 Examples
Fall 2015

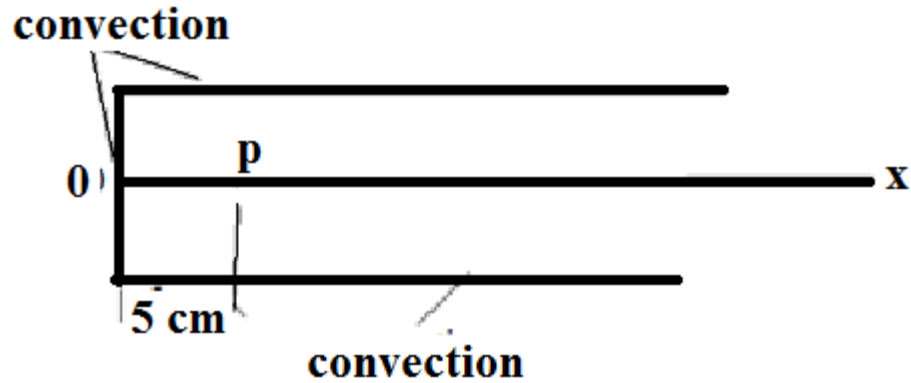
- 1) A solid copper sphere of 10-cm diameter [$\rho = 8954 \text{ kg/m}^3$, $c = 383 \text{ J/kg} \cdot ^\circ\text{C}$, $k = 386 \text{ W/m} \cdot ^\circ\text{C}$] initially at a uniform temperature $T_i = 250^\circ\text{C}$, is suddenly immersed in a well-stirred fluid which is maintained at a uniform temperature $T_\infty = 50^\circ\text{C}$. The heat transfer coefficient between the sphere and the fluid is $\bar{h} = 200 \text{ W/m}^2 \cdot ^\circ\text{C}$
 - (a) Check whether the lumped system analysis is suitable
 - (b) If it is suitable, determine the temperature of copper sphere at $t=5, 10$ and 20 min after the immersion.
- 2) A solid rod [$\alpha = 2 \times 10^{-5} \text{ m}^2/\text{s}$ and $k = 60 \text{ W/(m} \cdot ^\circ\text{C)}$] of diameter $D = 6 \text{ cm}$, initially at temperature $T_i = 800^\circ\text{C}$, is suddenly dropped into an oil bath at $T_\infty = 50^\circ\text{C}$. The heat transfer coefficient between the fluid and the surface is $h = 400 \text{ W/(m}^2 \cdot ^\circ\text{C)}$.
 - (a) Using the transient-temperature charts, determine the centerline temperature 10 min after immersion in the fluid.
 - (b) How long will it take the centerline temperature to reach 100°C ?Answer: (a) 54.5°C ; (b) 5 min 47 s
- 3) An orange of diameter 10 cm is initially at a uniform temperature of 30°C . It is placed in a refrigerator in which the air temperature is 2°C . If the transfer coefficient between the air and the surface of the orange is $h = 50 \text{ W/(m}^2 \cdot ^\circ\text{C)}$, determine the time required for the center of the orange to reach 10°C . Assume the thermal properties of the orange are the same as those of water at the same temperature. [$\alpha = 1.4 \times 10^{-7} \text{ m}^2/\text{s}$ and $k = 0.59 \text{ W/(m} \cdot ^\circ\text{C)}$]
Answer: 1 h 32 min
- 4) A steel plate [$\alpha = 1.2 \times 10^{-5} \text{ m}^2/\text{s}$ and $k = 43 \text{ W/(m} \cdot ^\circ\text{C)}$] of thickness $2L = 10 \text{ cm}$, initially at a uniform temperature of 240°C , is suddenly immersed in an oil bath $T_\infty = 40^\circ\text{C}$. The convection heat transfer coefficient between the fluid and the surface is $h = 600 \text{ W/(m}^2 \cdot ^\circ\text{C)}$. How long will it take for the center plane to cool to 100°C ? What fraction of the initial energy is removed during this time?
- 5) A thick concrete slab ($\alpha = 7 \times 10^{-7} \text{ m}^2/\text{s}$) is initially at a uniform temperature $T_i = 60^\circ\text{C}$. One of its surfaces is suddenly lowered to 10°C . By treating this as a one-dimensional transient heat conduction problem in a semi-infinite medium, determine the temperatures at depths 5 and 10 cm from the surface 30 min after the surface temperature is lowered.

- 6) A thick bronze [$\alpha = 0.86 \times 10^{-5} \text{ m}^2/\text{s}$ and $k = 26 \text{ W}/(\text{m} \cdot ^\circ\text{C})$] is initially at a uniform temperature 250°C . Suddenly the surface is exposed to a coolant 25°C . Assuming that the heat transfer coefficient for convection between the fluid and the surface is $150 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$, determine the temperature 5 cm from the surface 10 min after the exposure.
Answer: 205°C

- 7) A rectangular aluminum bar 6 cm by 3 cm [$k = 200 \text{ W}/(\text{m} \cdot ^\circ\text{C})$, $c_p = 890 \text{ J}/(\text{kg} \cdot ^\circ\text{C})$, $\rho = 2700 \text{ kg}/\text{m}^3$, and $\alpha = 8.4 \times 10^{-5} \text{ m}^2/\text{s}$] is initially at a uniform temperature $T_i = 175^\circ\text{C}$. Suddenly the surfaces are subjected to convective cooling with a heat transfer coefficient $h = 250 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ into an ambient at $T_\infty = 25^\circ\text{C}$ as shown in figure. Determine the center temperature T_o of the bar $t = 1 \text{ min}$ after the start of the cooling.
Answer: 107.5°C



- 8) A semi-infinite strip, $0 < x < \infty$, $0 < y < 10 \text{ cm}$, of fireclay brick [$k = 1 \text{ W}/(\text{m} \cdot ^\circ\text{C})$, and $\alpha = 5.4 \times 10^{-5} \text{ m}^2/\text{s}$] is initially at a uniform temperature $T_i = 340^\circ\text{C}$. Suddenly all surfaces are subjected to convection, with a heat transfer coefficient $h = 100 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ into an ambient at $T_\infty = 40^\circ\text{C}$. Calculate the temperature T_o of a point P located along the midplane at a distance $L = 5 \text{ cm}$ from the surface as shown in figure, $t = 2 \text{ h}$ after the start of the cooling.



Answer: 51.4 °C

- 9) A semi-infinite, cylindrical iron bar [$\alpha = 1.6 \times 10^{-5} \text{ m}^2/\text{s}$ and $k = 60 \text{ W}/(\text{m} \cdot ^\circ\text{C})$] of diameter $D = 5 \text{ cm}$, confined to the region $0 \leq x \leq \infty$, is initially at a uniform temperature $T_i = 330 ^\circ\text{C}$. Suddenly the surfaces are subjected to convection with a heat transfer coefficient $h = 200 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C})$ into an ambient at $T_\infty = 30 ^\circ\text{C}$. Determine the temperature T_0 of a point P located along the axis $L = 3 \text{ cm}$ from the flat surface $t = 2 \text{ min}$ after the start of the cooling. See figure given below.

